

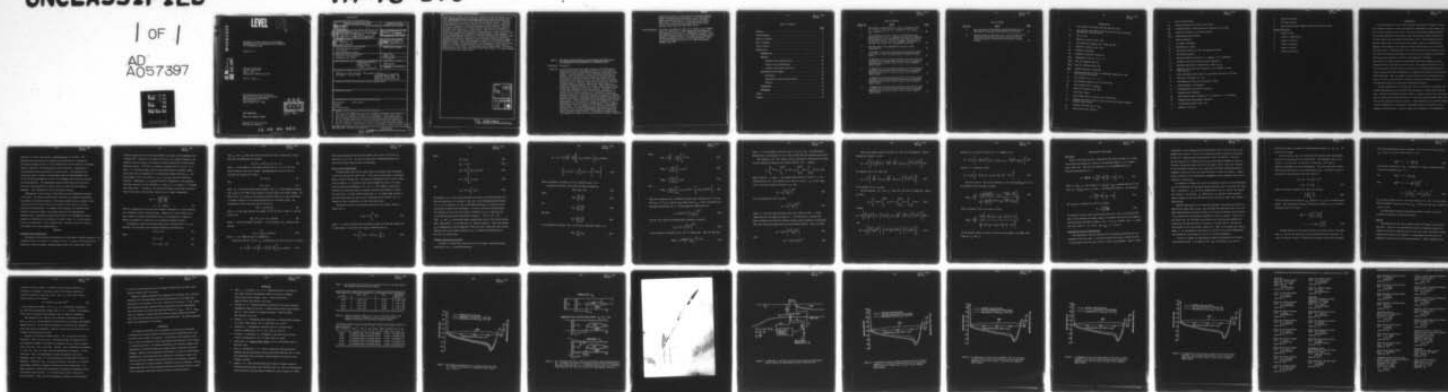
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HORIZONTAL BUOYANCY EFFECTS ON THE PRESSURE  
DISTRIBUTION OF AN AXISYMMETRIC BODY OPERATING  
IN A CYLINDRICAL DUCT

Lauchle, G. C.

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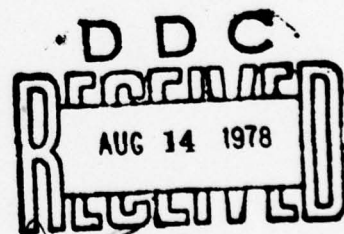
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| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number)<br>(U) It is well known that the static pressure coefficient values obtained from tests of axisymmetric bodies in, for example, a large water tunnel indicate the existence of tunnel wall interference. This interference is due to blockage experienced by the body operating within the boundaries of the test section walls, and to the skin friction on both the tunnel walls and the surface of the body, which in turn causes finite thickness boundary layers to develop. These factors result in a decrease in static pressure → |                       |  |

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along the test section which leads to a spurious horizontal buoyancy on the body. These interferences become more important as the size of the body increases relative to the fixed dimensions of the test section. Potential flow calculations can only account for solid blockage effects. A control volume analysis has thus been carried out from which pressure coefficient correction terms due to horizontal buoyancy have been obtained. They may be directly applied to any inviscid pressure distribution calculated for any given body operating in a given tunnel. These correction factors are computed for a large, streamlined body operating over a range of velocities, in The Pennsylvania State University, Garfield Thomas 1.22-m. diameter Water Tunnel. They are applied to a theoretically-determined potential flow, in-tunnel body pressure distribution to obtain the viscous flow pressure distributions which are compared to those determined experimentally. The agreement between theory and experiment is shown to be very good over all speeds considered. Traditional methods of accounting for horizontal buoyancy which are obtained from measurements of the longitudinal static pressure gradient in a clear tunnel, are applicable only to small bodies. The present method permits one to treat relatively large bodies which have a much stronger interaction with the tunnel walls.

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Subject: Horizontal Buoyancy Effects on the Pressure Distribution of an Axisymmetric Body Operating in a Cylindrical Duct

References: See page 26

Abstract: It is well known that the static pressure coefficient values obtained from tests of axisymmetric bodies in, for example, a large water tunnel indicate the existence of tunnel wall interference. This interference is due to blockage experienced by the body operating within the boundaries of the test section walls, and to the skin friction on both the tunnel walls and the surface of the body, which in turn causes finite thickness boundary layers to develop. These factors result in a decrease in static pressure along the test section which leads to a spurious horizontal buoyancy on the body. These interferences become more important as the size of the body increases relative to the fixed dimensions of the test section. Potential flow calculations can only account for solid blockage effects. A control volume analysis has thus been carried out from which pressure coefficient correction terms due to horizontal buoyancy have been obtained. They may be directly applied to any inviscid pressure distribution calculated for any given body operating in a given tunnel. These correction factors are computed for a large, streamlined body operating over a range of velocities in The Pennsylvania State University, Garfield Thomas 1.22-m. diameter Water Tunnel. They are applied to a theoretically-determined potential flow, in-tunnel body pressure distribution to obtain the viscous flow pressure distributions which are compared to those determined experimentally. The agreement between theory and experiment is shown to be very good over all speeds considered.

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## Nomenclature

|                     |   |
|---------------------|---|
| $A$                 | the blocked area between the body and duct wall   |
| $A_e$               | the effective area between the body and duct wall including displacement thickness effect |
| $A_o$               | area of duct  |
| $a$                 | numerical constant in Eq. (46)  |
| $B_i$               | the continuity integral, Eq.'s (40) and (41)  |
| $C_o$               | numerical constant in Eq. (46)  |
| $C_p$               | pressure coefficient  |
| $\Delta C_p$        | pressure coefficient correction   |
| $\Delta C_{p_i}$    | components of $\Delta C_p$ ( $i = 1, 2, \dots$ )  |
| $\Delta C_{p_{11}}$ | $\Delta C_{p_1}$ for laminar-body flow  |
| $\Delta C_{p_{12}}$ | $\Delta C_{p_1}$ for turbulent-body flow  |
| $D_{max}$           | maximum diameter of the body  |
| $d_o$               | distance from nose of body to geometrical beginning of the water tunnel test section      |
| $F_i$               | fluid forces ( $i = 1, 2, \dots$ )  |
| $I_i$               | the momentum integral, Eq.'s (37) and (38)  |
| $K_n$               | body fineness ratio ( $l_n/D_{max}$ )   |
| $k$                 | numerical constant in Eq. (46)  |
| $L$                 | total body length   |
| $l$                 | duct length used in potential flow calculation  |
| $l_o$               | distance from nose of body to point on duct wall where turbulent boundary layer begins    |
| $l_n$               | distance from body nose to $D_{max}$  |
| $P_o$               | free-stream static pressure   |

|              |   |
|--------------|---|
| $p$          | local fluid pressure  |
| $p_b$        | pressure exerted by the body on the fluid                                   |
| $p'_b$       | "displaced-body" pressure exerted by the body on the fluid                  |
| $R_L$        | radius of curvature of the body tailcone                                    |
| $Re_L$       | body-length Reynolds number   |
| $r$          | radius coordinate   |
| $s$          | arc length coordinate   |
| $s_t$        | transition arc length   |
| $U_\infty$   | free-stream velocity in duct far upstream of body                           |
| $u$          | local fluid velocity  |
| $u_i$        | velocity profile for body ( $i = 1$ , laminar; $i = 2$ , turbulent)         |
| $u_o$        | reference velocity in potential flow computation                            |
| $u_r$        | numerical rake output far upstream of body ( $U_\infty/u_o$ )               |
| $u_{rp}$     | numerical rake output near the body at, for example, a pitot probe location |
| $x$          | axial coordinate where origin is $\ell_o$ upstream from nose of the body    |
| $\bar{x}$    | body axial coordinate ( $x - \ell_o$ )                                      |
| $\bar{x}$    | non-dimensional body axial coordinate ( $\bar{x}/\ell_n$ )                  |
| $x'$         | dummy variable of integration   |
| $\hat{y}$    | non-dimensional body radius ( $r_b/D_{\max}/2$ )                            |
| $\delta$     | boundary-layer thickness  |
| $\delta_i$   | body boundary-layer thickness ( $i = 1$ , laminar; $i = 2$ , turbulent)     |
| $\delta^*$   | boundary-layer displacement thickness                                       |
| $\epsilon_L$ | the expression given by Eq. (47)  |
| $\nu$        | kinematic viscosity   |

$\rho$  fluid mass density  
 $\tau$  wall shear stress  
 $\phi$  angle formed between tangent line of body and the x-axis

Special Subscripts

b refers to body  
E refers to experimental  
I refers to inviscid  
m refers to measured  
V refers to viscous  
w refers to duct wall



## INTRODUCTION

The investigation of flows about bodies of revolution in cylindrical ducts is of general interest to those concerned with turbomachinery, wind tunnel, and water tunnel testing, to note a few. There have been several methods proposed for the determination of the potential flow about bodies operated within ducts of both constant and non-uniform cross section [1-5]. These methods allow for blockage effects due to the duct (or test section) walls to be accounted for. However, these methods do not allow for viscous effects that occur on the body and tunnel walls. Viscosity gives rise to skin friction on all surfaces in contact with the flowing fluid; which, in turn gives rise to boundary layer growth. The displacement thickness varies from the beginning of boundary layer growth to distant points far downstream, effectively changing the cross-sectional areas of both the body and the duct. This added constriction of the flow and the skin friction creates a second type of blockage characterized by a static pressure drop from the beginning of boundary layer growth to any arbitrary point downstream. This net change in static pressure may be interpreted in the form of a force in the horizontal direction (assuming the tunnel test section is horizontal) which is the so-called "horizontal buoyancy."

In many applications, it is necessary to know as precisely as possible, the pressure distribution on a particular body operating in a given tunnel test section. Because of horizontal buoyancy effects, a typical inviscid flow calculation will not yield totally accurate results for relatively large diameter bodies (relative to the diameter of the test section). This statement may be verified through a direct comparison of experimentally determined pressure distributions with a potential flow prediction. Figure 1 shows such a comparison. The axisymmetric

body here is 3.05-m. long and has a maximum diameter of 32.39-cm. The pressure coefficient data were obtained on this body while it operated in the Garfield Thomas 48-inch (1.22-m.) diameter Water Tunnel located at the Applied Research Laboratory of The Pennsylvania State University. A description of the experiments will be presented in a later section. The potential flow calculation shown in Figure 1 was performed using the Douglas-Neumann code [1,2]. The solid blockage due to the 1.22-m. diameter test section is included in this computation. The experimental pressure coefficients are seen to be lower than those predicted at a given point on the body and are velocity-dependent. This discrepancy is due to horizontal buoyancy.

Measurements of body pressure distributions are not economically practical in all cases. The next best alternative, therefore is to approach analytically the problem of horizontal buoyancy. This report presents such an analysis, where correction terms are derived that may be applied to the results of a given potential flow calculation. As examples of the analysis, we include calculations for the body of Figure 1 and compare them with the experimentally determined data. Although the analysis given here is for axisymmetric bodies operating in cylindrical test sections of constant radius, it is quite general so that its adaptation to other configurations (variable radius test sections, for example) would seem straightforward.

## ANALYSIS

### Potential Flow Considerations

The potential flow pressure distribution on an arbitrarily-shaped axisymmetric body operating within the confines of a cylindrical duct of circular cross section may be calculated using the Douglas-Neumann computer code [1,2], among others [3-5].

A typical computation with the Douglas-Neumann code might use the modeling shown in Figure 2(a). Because of the limited core size on our digital computers, the length of the duct (which is described by discrete points) must be finite when using this method. If the duct is assumed to extend from  $\bar{x} = -\ell$  to  $\bar{x} = \ell + L$ , where  $L$  is the body length, then the resulting pressure coefficient values on the body ( $C_p$ ) are normalized to an unspecified reference velocity,  $u_o$ . We know, however, that in the limit  $\ell \rightarrow \infty$ ,  $u_o \rightarrow U_\infty$  ( $U_\infty$  is the true velocity at infinity). Consequently, in conjunction with our computation of the potential flow about the body, we also determine  $u_r \equiv U_\infty/u_o$  at  $\bar{x} = -\ell$ , where  $\ell$  is assumed much larger than  $L$ . Knowing  $u_r$ , the calculated pressure coefficient values may then be corrected to the reference velocity  $U_\infty$  by a simple computation:

$$\begin{aligned} C_{p_I} &= 1 - \left( \frac{u_I}{u_o} \right)^2 \left( \frac{u_o}{U_\infty} \right)^2 \\ &= 1 - (1 - C_p)/u_r^2 \end{aligned} \quad (1)$$

where  $C_{p_I}$  represents the potential flow pressure coefficient on a body operating in a cylindrical tube of infinite extent. Equation (1) is most useful to use when a number of pressure distributions are to be calculated for a family of bodies and compared; it assures us of a consistent reference velocity.

By defining a control volume from Figure 2(a) to extend from  $\bar{x} = -\infty$  to an arbitrary  $\bar{x}$  on the body, the continuity equation may be written as

$$A_o U_\infty = A u_I \quad (2)$$

where

$$A_o = \pi r_w^2 \quad (3)$$

$$A = \pi (r_w^2 - r_b^2) \quad (4)$$



with  $r_w$  and  $r_b$  being the tunnel wall and body radii, respectively. We may also write the momentum flux equation:

$$\rho u_I^2 A - \rho U_\infty^2 A_o = F_1 + F_2 + F_3, \quad (5)$$

where  $\rho$  is the density of the fluid, and the  $F_i$ 's ( $i = 1, 2, 3$ ) are the forces acting on the control volume. Assuming positive forces to act in the positive  $x$ -direction, we have:

$$F_1 = P_o A_o \quad (6)$$

and

$$F_2 = -p_I A, \quad (7)$$

where  $P_o$  is the free-stream static pressure, and  $p_I$  is the potential pressure that occurs in the fluid at any arbitrary location within the control volume. The third force,  $F_3$  is due to the pressure exerted by the body in the  $x$ -direction. It depends therefore on the pressure distribution of the body,  $p_b(\bar{x})$ . The differential form of this force may be written as

$$dF_3 = -p_b \sin\phi dA_b, \quad (8)$$

where  $\phi$  is the angle between the tangent line of the body at point  $\bar{x}$  and the  $\bar{x}$ -axis, and

$$dA_b = 2\pi r_b ds = 2\pi r_b d\bar{x}/\cos\phi, \quad (9)$$

where  $s$  is the arc-length coordinate. We can integrate  $dF_3$  along the body and get

$$F_3 = -2\pi \int_0^{\bar{x}} p_b r_b \tan\phi dx', \quad (10)$$

where  $x'$  is a dummy variable of integration.

We may now solve Eq. (5) for  $p_I$  (contained in  $F_2$ ) and use Eq. (2) to obtain:

$$p_I = P_o \frac{A_o}{A} - \rho U_\infty^2 \frac{A_o^2}{A^2} + \rho U_\infty^2 \frac{A_o}{A} - \frac{2\pi}{A} \int_0^{\bar{x}} p_b r_b \tan\phi dx'. \quad (11)$$



This equation describes the inviscid pressure that occurs in the fluid at location  $\bar{x}$  ( $0 \leq \bar{x} \leq L$ ). We will now derive the corresponding equation for this pressure when viscous effects are included.

#### Viscous Flow Considerations

Viscosity gives rise to wall shear stress and boundary layer development on both the body and the tunnel wall. A new control volume must be considered which is shown in Figure 2(b). We choose the beginning of this control volume to be a distance  $\ell_0$  upstream of the forward stagnation point of the body, where the new axial coordinate  $x = \bar{x} + \ell_0 = 0$ . This origin is judiciously selected to be the point where a turbulent boundary layer begins to form on the tunnel wall. We will further assume that  $\ell_0$  is large enough relative to the body length such that the velocity is uniform across the duct at  $x = 0$ . Without any loss of generality, we call this velocity  $U_\infty$ .

The general form of the continuity equation for the control volume of Figure 2(b) is

$$A_0 U_\infty = 2\pi \int_{r_b}^{r_w} u r dr, \quad (12)$$

where  $u$  is the non-uniform velocity profile between the body and tunnel wall.

In like manner, we can write the change in momentum flux as

$$2\pi \rho \int_{r_b}^{r_w} u^2 r dr - \rho U_\infty^2 A_0 = \sum_{i=4}^8 F_i, \quad (13)$$

where

$$F_4 = P_o A_o \quad , \quad (14)$$

$$F_5 = - P_v A \quad , \quad (15)$$

$$F_6 = -2\pi \int_{\ell_o}^x p'_b r_b \tan\phi \, dx' \quad , \quad (16)$$

$$F_7 = -2\pi \int_{\ell_o}^x r_b \tau_b \, dx' \quad , \quad (17)$$

and

$$F_8 = -2\pi r_w \int_0^x \tau_w \, dx' \quad . \quad (18)$$

The quantity  $p_v$  is the viscous pressure that occurs in the fluid between the body and tunnel wall at location  $x$ , and  $p'_b$  is the "displaced-body" pressure, i.e., it is a perturbed  $p_b$  due to the added acceleration of the flow caused by the body boundary-layer development. It may be calculated using potential flow methods, but with the body radius re-defined by  $r'_b = r_b + \delta_b^*$ , where  $\delta_b^*$  is the body boundary-layer displacement thickness. In Eq.'s (17) and (18),  $\tau_b$  and  $\tau_w$  are the wall shear stresses that occur on the body and tunnel wall, respectively. It is noted that  $F_7$  does not contain a  $\cos\phi$  term because  $F_7$ , by assumption, is the x-component of the force due to body wall shear stress. Equation (13) can be readily solved for  $p_v$  to obtain an analogous form of Eq. (11) for viscous flow.

#### Pressure Coefficient Correction

To obtain a viscous flow correction for the in-tunnel, inviscid pressure coefficient,  $C_{p_I}$ , we form the difference

$$p_V - p_I = \rho U_\infty^2 \frac{A_o^2}{A^2} + \frac{2\pi}{A} \left\{ \int_{\ell_o}^x p_b r_b \tan\phi \, dx' - \int_{\ell_o}^x p'_b r_b \tan\phi \, dx' \right. \\ \left. - \int_{\ell_o}^x r_b \tau_b \, dx' - r_w \int_0^x \tau_w \, dx' - \rho \int_{r_b}^{r_w} u^2 r \, dr \right\} , \quad (19)$$

where the change of variable  $x = \bar{x} + \ell_o$  was made in Eq. (11).

A pressure coefficient correction term may be defined by:

$$\Delta C_p = C_{p_V} - C_{p_I} , \quad (20)$$

where

$$C_{p_V} = \frac{p_V - p_o}{\frac{1}{2} \rho U_\infty^2} , \quad (21)$$

and

$$C_{p_I} = \frac{p_I - p_o}{\frac{1}{2} \rho U_\infty^2} , \quad (22)$$

such that

$$\Delta C_p = \frac{p_V - p_I}{\frac{1}{2} \rho U_\infty^2} . \quad (23)$$

It is convenient to express  $\Delta C_p$  as the sum of individual terms, i.e.,

$$\Delta C_p = \sum_{i=1}^4 \Delta C_{p_i} , \quad (24)$$

where

$$\Delta C_{p1} = 2 \frac{A_o^2}{A^2} - \frac{4\pi}{A U_\infty^2} \int_{r_b}^{r_w} u^2 r dr, \quad (25)$$

$$\Delta C_{p2} = - \frac{4\pi}{A \rho U_\infty^2} \int_{\ell_o}^x r_b \tau_b dx', \quad (26)$$

$$\Delta C_{p3} = - \frac{4\pi r_w}{A \rho U_\infty^2} \int_0^x \tau_w dx', \quad (27)$$

and

$$\Delta C_{p4} = \frac{4\pi}{A \rho U_\infty^2} \left\{ \int_{\ell_o}^x p_b r_b \tan\phi dx' - \int_{\ell_o}^x p_b' r_b \tan\phi dx' \right\}. \quad (28)$$

Under the assumption that a turbulent boundary layer originates at  $x = 0$ , and that  $(\ell_o + L) \lesssim 10 r_w$ , then the wall shear stress,  $\tau_w$ , can be calculated from flat-plate expressions [6, 7]. After making the substitution [6]

$$\tau_w = 0.0225 \rho U_\infty^2 \left( \frac{\nu}{U_\infty \delta_w} \right)^{1/4} \quad (29)$$

into Eq. (27), where the boundary-layer thickness is given by

$$\delta_w = 0.37 x \left( \frac{U_\infty x}{\nu} \right)^{-1/5}, \quad (30)$$

we can evaluate the integral of Eq. (27) in closed form. Thus, we find that

$$\Delta C_{p3} = -r_w \frac{0.144 \pi}{A} \left( \frac{\nu}{U_\infty} \right)^{1/5} x^{4/5}, \quad (31)$$



where  $\nu$  is the kinematic viscosity, and  $A = A_0$  for  $x \leq x_0$ . For arbitrarily-shaped bodies, the integrals of Eq.'s (26) and (28) must be evaluated numerically.

The integral of Eq. (25), however, may be evaluated in closed form if we make certain assumptions regarding the velocity profile  $u(r)$ . Clearly,

$$I_i \equiv \int_{r_b}^{r_w} u^2 r dr = \int_{r_b}^{r_b + \delta_i} u_i^2 r dr + u_v^2 \int_{r_b + \delta_i}^{r_w - \delta_w} r dr + \int_{r_w - \delta_w}^{r_w} u_w^2 r dr, \quad (32)$$

where subscript  $i$  equals 1 for laminar-body flow and is equal to 2 for turbulent-body flow. The boundary-layer velocity profile,  $u_w$ , at the tunnel wall is (as above) assumed turbulent, i.e., [6],

$$u_w = u_v \left( \frac{r_w - r}{\delta_w} \right)^{1/7}. \quad (33)$$

On the turbulent-flow body, we have:

$$u_2 = u_v \left( \frac{r - r_b}{\delta_2} \right)^{1/7}, \quad (34)$$

where  $\delta_2$  is of the same analytical form as Eq. (30), but with  $x$  being replaced by the arc length coordinate,  $s$ . For the case of a laminar-flow body we assume a sine function velocity profile, which according to Schlichting [6], very accurately approximates the exact Blasius profile. Thus, we assume

$$u_1 = u_v \sin \left( \frac{\pi (r - r_b)}{2 \delta_1} \right), \quad (35)$$

with

$$\delta_1 = 4.7953 (\nu s / U_\infty)^{1/2}. \quad (36)$$

With these assumed velocity profiles, Eq. (32) can be integrated. Without showing the details, we find:

$$I_1 = u_V^2 \left\{ \left( \frac{4 - \pi^2}{4\pi^2} \right) \delta_1^2 - \frac{r_b \delta_1}{2} + \frac{\delta_w^2}{16} - \frac{2}{9} r_w \delta_w + \left( \frac{r_w^2 - r_b^2}{2} \right) \right\} \quad (37)$$

for laminar flow on the body, and

$$I_2 = u_V^2 \left\{ -\frac{\delta_2^2}{16} - \frac{2}{9} r_b \delta_2 + \frac{\delta_w^2}{16} - \frac{2}{9} r_w \delta_w + \left( \frac{r_w^2 - r_b^2}{2} \right) \right\} \quad (38)$$

for turbulent flow on the body.

We now eliminate  $u_V^2$  from  $I_1$ ; thus, Eq. (12) must be integrated. Again, we write

$$B_1 \equiv \int_{r_b}^{r_w} u \, r \, dr = \int_{r_b}^{r_b + \delta_1} u_1 \, r \, dr + u_V \int_{r_b + \delta_1}^{r_w - \delta_w} r \, dr + \int_{r_w - \delta_w}^{r_w} u_w \, r \, dr, \quad (39)$$

finding

$$B_1 = u_V \left\{ \left( \frac{8 - \pi^2}{2\pi^2} \right) \delta_1^2 + \left( \frac{2 - \pi}{\pi} \right) r_b \delta_1 + \frac{\delta_w^2}{30} - \frac{r_w \delta_w}{8} + \left( \frac{r_w^2 - r_b^2}{2} \right) \right\} \quad (40)$$

and

$$B_2 = u_V \left\{ \left( \frac{\delta_w^2 - \delta_2^2}{30} \right) - \left( \frac{r_w \delta_w + r_b \delta_b}{8} \right) + \left( \frac{r_w^2 + r_b^2}{2} \right) \right\} \quad (41)$$

Because  $B_1 = A_o U_\infty / 2\pi$  we obtain for  $i = 1$  (laminar flow):

$$u_V = A_o U_\infty \left\{ A - \left( \frac{8 - \pi^2}{\pi} \right) \delta_1^2 + 2(2 - \pi) r_b \delta_1 - \frac{\pi r_w \delta_w}{4} + \frac{\pi}{15} \delta_w^2 \right\}^{-1} \quad (42)$$

and for  $i = 2$  (turbulent flow):

$$u_V = A_o U_\infty \left\{ A - \frac{\pi}{4} (r_b \delta_2 + r_w \delta_w) + \frac{\pi}{15} (\delta_w^2 - \delta_2^2) \right\}^{-1} \quad (43)$$

The first term of  $\Delta C_p$  may be expressed in the form  $\Delta C_{p1} = \Delta C_{p11}$  ( $i=1$  or  $2$ ).

For laminar flow on the body, we find:

$$\Delta C_{p11} = \frac{A_o^2}{A^2} - \frac{2A_o^2 \left\{ A + \left( \frac{4 - \pi^2}{2\pi} \right) \delta_1^2 - \pi r_b \delta_1 - \frac{4\pi r_w \delta_w}{9} + \frac{\pi \delta_w^2}{8} \right\}}{A \left\{ A - \left( \frac{8 - \pi^2}{\pi} \right) \delta_1^2 + 2(2 - \pi) r_b \delta_1 - \frac{\pi r_w \delta_w}{4} + \frac{\pi}{15} \delta_w^2 \right\}^2} \quad (44)$$

and for turbulent flow on the body, we find:

$$\Delta C_{p12} = \frac{A_o^2}{A^2} - \frac{2A_o^2 \left\{ A - \frac{4\pi}{9} (r_w \delta_w + r_b \delta_2) + \frac{\pi}{8} (\delta_w^2 - \delta_2^2) \right\}}{A \left\{ A - \frac{\pi}{4} (r_w \delta_w + r_b \delta_2) + \frac{\pi}{15} (\delta_w^2 - \delta_2^2) \right\}^2} \quad (45)$$

If the boundary layers are thin, one may of course neglect the higher order terms in  $\delta_w$  and  $\delta_1$ .

# APPLICATION OF THE THEORY

## Body Shape

Based on the above analysis, computations have been performed for a large, streamlined body designed to operate in the Garfield Thomas 1.22-m. diameter Water Tunnel [8]. This body was referred to in the INTRODUCTION and is described mathematically by:

$$\hat{y} = \sqrt{\hat{x}(2-\hat{x})} - K_n \frac{C_o \hat{x}}{2a^2} \exp\left\{-\frac{\hat{x}^2}{2a^2} - k K_n\right\} + \hat{x}^2 \epsilon_L, \quad (46)$$

where  $\hat{x} = x/\ell_n$ ,  $\ell_n$  = nose length,  $\hat{y} = r_b/D_{\max}/2$ ,  $D_{\max}$  = maximum diameter of the body,  $K_n = \ell_n/D_{\max}$ , and  $a$ ,  $C_o$ , and  $k$  are numerical constants. The parameter

$$\epsilon_L = \frac{K_n C_o}{2a^2} \exp\left\{-\frac{1}{2a^2} - k K_n\right\}. \quad (47)$$

The tailcone is formed by an  $18^\circ$  arc of radius

$$R_L = \frac{2.5 D_{\max}}{2 \sin 18^\circ}. \quad (48)$$

An inflection curve is then faired between the end of the arc (at  $\phi=90-18=72^\circ$ ) and a 4-inch diameter disk whose center is coincident with the axis of symmetry. This body shape was shown in Figure 1 for  $a = 0.3$ ,  $C_o = 0.0303$ , and,  $k = 0.45227$ . The total length,  $L$ , is 3.05-m., and  $D_{\max}$  is 32.39 cm.

## Experimental Pressure Distributions

The experimental body was manufactured by building up multiple layers of fiberglass cloth and resin. A precision template was used to screed the body to final shape before the last coating of resin fully hardened. Figure 3 shows



a photograph of the completed body and sting mount used to hold it in the 1.22-m. diameter test section. A total of 94 pressure taps were located in the surface of the body. These pressure orifices were 0.79-mm. in diameter. Each body tap was connected to a flexible plastic tube which passed through the inside of the body, through the sting, and out of the tunnel. The 94 tubes then connected to two 48-channel Scanivalves and a single Bell and Howell calibrated pressure transducer. Before all runs, the tubes were bled to remove air pockets. Figure 4 shows a schematic of the experimental arrangement and the equations used in data reduction to obtain  $C_{p_E}$ .

As indicated in Figures 2(c) and 4 the reference velocity in the measurements,  $u_m$ , was obtained with a pitot probe placed relatively close to the body and tunnel wall. Consequently,  $u_m$  may not be interpreted as the  $U_\infty$  used in the theoretical analysis. The velocity  $u_m$  differs from  $U_\infty$  because of both potential effects induced by the body and viscous effects created by tunnel wall boundary-layer growth.

Detailed measurements of the turbulent boundary layer growth on the wall of the Garfield Thomas Water Tunnel were performed and reported by Ross, et al [7]. They concluded that an effective origin for the start of boundary layer growth is  $1.5 r_w$  upstream from the geometric beginning of the test section. That is, one may assume that the cylindrical test section can be fictitiously extended upstream into the settling section a distance  $1.5 r_w$  and refer to this point as the entrance of the test section, Figure 2(c). Thus, we can assume  $l_o = 1.5 r_w + d_o$ , where  $d_o$  is the distance from the nose of the body to the actual beginning of the cylindrical test section ( $d_o = 54.6$  cm. in this arrangement).

In order to compare our experimental pressure distributions with theoretically predicted ones, it is apparent that  $C_{p_E}$  (referenced to  $u_m$ ) must be

corrected in order to account for the differences between  $u_m$  and  $U_\infty$ . We do this in two steps.

We first correct  $Cp_E$  for the tunnel wall boundary-layer displacement thickness at the position of the pitot probe. This thickness varies from 2.02-mm. at 15.24 m./sec. to 2.42-mm. at 6.09m./sec. (the range of velocities considered in this investigation). The pitot probe was 4-inches from the wall and thus was out of the boundary layer. The effective area of the tunnel at the position of the pitot probe is:

$$\begin{aligned} A_e &= A_o - 2\pi r_w \delta_w^* + \pi \delta_w^2 \\ &\approx A_o - 2\pi r_w \delta_w^* \end{aligned} \quad (49)$$

From the continuity equation [Eq. (12)], we can write

$$\left( \frac{u_m}{U_\infty} \right)_V = \frac{A_o}{A_e}, \quad (50)$$

which represents the increase in  $u_m$  relative to  $U_\infty$  due to boundary-layer growth. The experimental pressure coefficient corrected to  $U_\infty$  by viscous considerations only is thus:

$$\begin{aligned} Cp_E^V &= 1 - \left( \frac{u_E}{u_m} \right)^2 \left( \frac{u_m}{U_\infty} \right)_V^2 \\ &= 1 - (1 - Cp_E) \left( \frac{A_o}{A_e} \right)^2 \end{aligned} \quad (51)$$

We know (because of the close proximity of the pitot probe to the body) that  $u_m$  may also be influenced by the potential effects of the body. In order to correct for this, a potential flow solution, such as that obtained

from the Douglas-Neumann code is required. We calculate the velocity ratio  $u_{rp} = U_{\infty}/u_m$  at the pitot probe location. Then,

$$Cp_E^{cor.} = 1 - (1 - Cp_E^V)/u_{rp}^2 \quad (52)$$

is the final correction of  $Cp_E$ . Furthermore it makes no difference which correction is applied first, i.e.,

$$\text{let } Cp_E^I = 1 - (1 - Cp_E)/u_{rp}^2 ,$$

$$\text{then } Cp_E^{cor.} = 1 - (1 - Cp_E^I) \left( \frac{A_o}{A_e} \right)^2 ,$$

$$= 1 - \left( \frac{A_o}{A_e u_{rp}} \right)^2 + Cp_E \left( \frac{A_o}{A_e u_{rp}} \right)^2 . \quad (53)$$

It is easily verified that Eq. (52) also reduces to Eq. (53). For the experimental arrangement used here, we found  $u_{rp} = 0.9976$ , and that  $A_o/A_e$  ranges from 1.013 to 1.016.

The experimental pressure distributions shown in Figure 1 have been corrected according to the above discussion.

### Results

The generality of the above analysis allows both laminar and turbulent-body flow. As part of the experimental program, we therefore measured the laminar-to-turbulent transition points at the four tunnel velocities in which pressure distributions were measured. A wedge-shaped hot-film probe and anemometer system were used in these measurements. TABLE I summarizes the

transition location results. For those body coordinates forward of  $s_t$  (transition arc length), the laminar form of the pressure coefficient correction analysis is used [Eq. (44)]. And,  $\tau_b$  in Eq. (26) is calculated according to the formula

$$\tau_b = 0.332 \rho \nu U_\infty (U_\infty / \nu s)^{1/2} \quad (54)$$

in this laminar-flow regime. For  $s > s_t$ ,  $\tau_b$  is calculated according to Eq. (29) with the appropriate change from  $x$  to  $s$  variable. The integral of Eq. (26) is evaluated using Simpson's Rule of numerical integration.

The integrals of Eq. (28) are also evaluated using Simpson's Rule. Both  $p_b$  and  $p'_b$  are determined from the body-in-a cylindrical duct Douglas-Neumann solution. In this numerical example we calculated  $\delta_b^*$  (needed to obtain  $p'_b$ ) using an axisymmetric, implicit finite-difference solution of the boundary layer equations of motion.

Because of the thicker boundary layers,  $\Delta C_p$  is largest at the lower velocities. Thus, at 6.09 m./sec. a few typical values of  $\Delta C_{p_i}$  ( $i=1,2,3,4$ ) are presented in TABLE II from which an assessment of each  $\Delta C_{p_i}$ 's contribution to the total  $\Delta C_p$  can be made. Clearly,  $\Delta C_{p_3}$  contributes the greatest to  $\Delta C_p$ , but  $\Delta C_{p_1}$  and  $\Delta C_{p_2}$  are also significant contributors. On the other hand,  $\Delta C_{p_4}$  is approximately an order of magnitude lower than  $\Delta C_{p_2}$  ( $\Delta C_{p_2} < \Delta C_{p_1} < \Delta C_{p_3}$ ) for those locations on the body where the flow is turbulent. Obviously,  $\Delta C_{p_4}$  is the most tedious to calculate, so it may be conveniently justified to neglect it entirely from the computations. For those conditions in which the computations are compared to experimental data, this deletion has been made. It is further noted, that if body-flow is entirely laminar,  $\Delta C_{p_2}$  may also be neglected; although, we have retained



it for all of the computations in this example because there is only a small regime of laminar flow on the body.

Figures 5 through 8 summarize the comparisons of potential flow, corrected potential flow, and experimental pressure distributions for our given body operating at 6.09 through 15.24 m./sec. test-section velocities. At all speeds the horizontal buoyancy correction theory agrees well with the experimental data, particularly for those body positions forward of  $C_{p_{min}}$ . Aft of  $C_{p_{min}}$ , there is a region of strong interaction where coupling between the boundary-layer flow and the potential outer flow becomes important. The theory presented here is not applicable to this region.

#### CONCLUSIONS

The analysis presented here is applicable to many practical problems involving the flow about bodies of revolution within cylindrical ducts, such as wind or water tunnel test sections. In particular, this analysis allows one to correct an inviscid, in-duct body pressure distribution for the effects of horizontal buoyancy. The derived expressions are relatively simple; thus, computations are performed using very simple Fortran or desk-top calculator programs. Based on the experimental observations of, and on the computations performed for a particular body that operates in a given water tunnel test section, horizontal buoyancy effects were shown to be important and should not be neglected if precise pressure coefficient values are required. We have demonstrated that the theory adequately predicts the observed effects, except in the afterbody region where strong interaction effects dominate.

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Table I The experimentally determined transition points on the body used in the pressure distribution measurements.

| Tunnel Velocity<br>$U_{\infty}$<br>(m./sec.) | Body-Length Reynolds No.<br>$Re_L = U_{\infty} L / \nu$ | Transition Point<br>$s_t / L$ | Transition Reynolds No.<br>$Re_L (s_t / L)$ |
|--|---|-------------------------------|---|
| 6.09   | $1.88 \times 10^7$                                      | 0.150                         | $2.82 \times 10^6$                          |
| 9.14   | $2.83 \times 10^7$                                      | 0.116                         | $3.28 \times 10^6$                          |
| 12.19  | $3.76 \times 10^7$                                      | 0.100                         | $3.76 \times 10^6$                          |
| 15.24  | $4.72 \times 10^7$                                      | 0.083                         | $3.93 \times 10^6$                          |

Table II Typical values for  $\Delta C_{p_i}$  ( $i = 1, 2, 3, 4$ ) at 6.09 m./sec., the inviscid pressure coefficient, and the corrected inviscid pressure coefficient for horizontal buoyance effects.

| Body Coordinate<br>$\bar{x}/L = (x - \ell_0)/L$ | $\Delta C_{p_1}$ | $\Delta C_{p_2}$ | $\Delta C_{p_3}$ | $\Delta C_{p_4}$ | $\Delta C_p = \sum_{i=1}^4 \Delta C_{p_i}$ | $C_{p_I}$ | $C_{p_V}$ |
|---|------------------|------------------|------------------|------------------|--|-----------|-----------|
| 0.002   | -0.0038          | 0.000            | -0.0139          | 0.00009          | -0.0177                                    | 0.433     | 0.415     |
| 0.075   | -0.0046          | -0.00003         | -0.0158          | 0.00047          | -0.0199                                    | -0.036    | -0.056    |
| 0.253   | -0.0065          | -0.0006          | -0.0202          | 0.00061          | -0.0267                                    | -0.087    | -0.113    |
| 0.497   | -0.0091          | -0.0020          | -0.0261          | 0.00069          | -0.0366                                    | -0.139    | -0.176    |
| 0.667   | -0.0108          | -0.0031          | -0.0300          | 0.00071          | -0.0432                                    | -0.161    | -0.204    |

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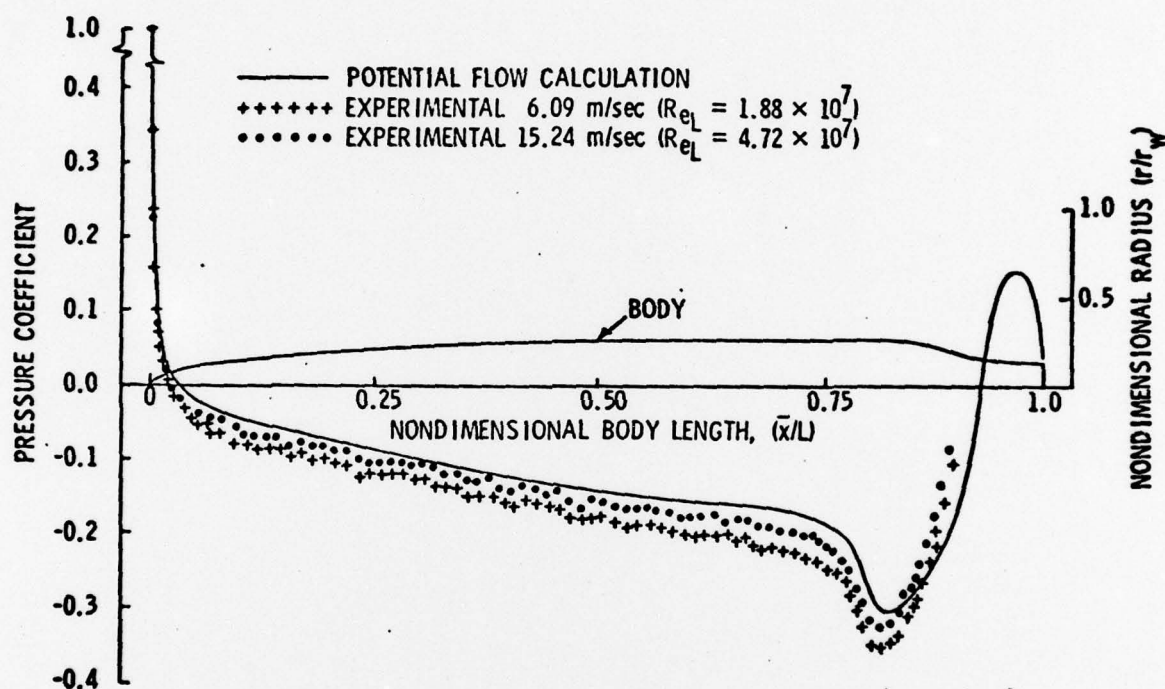


Figure 1 The pressure distributions on a large axisymmetric body ( $L = 3.05$ -m.) operating in a cylindrical test section ( $r_w = 1.22$ -m.)



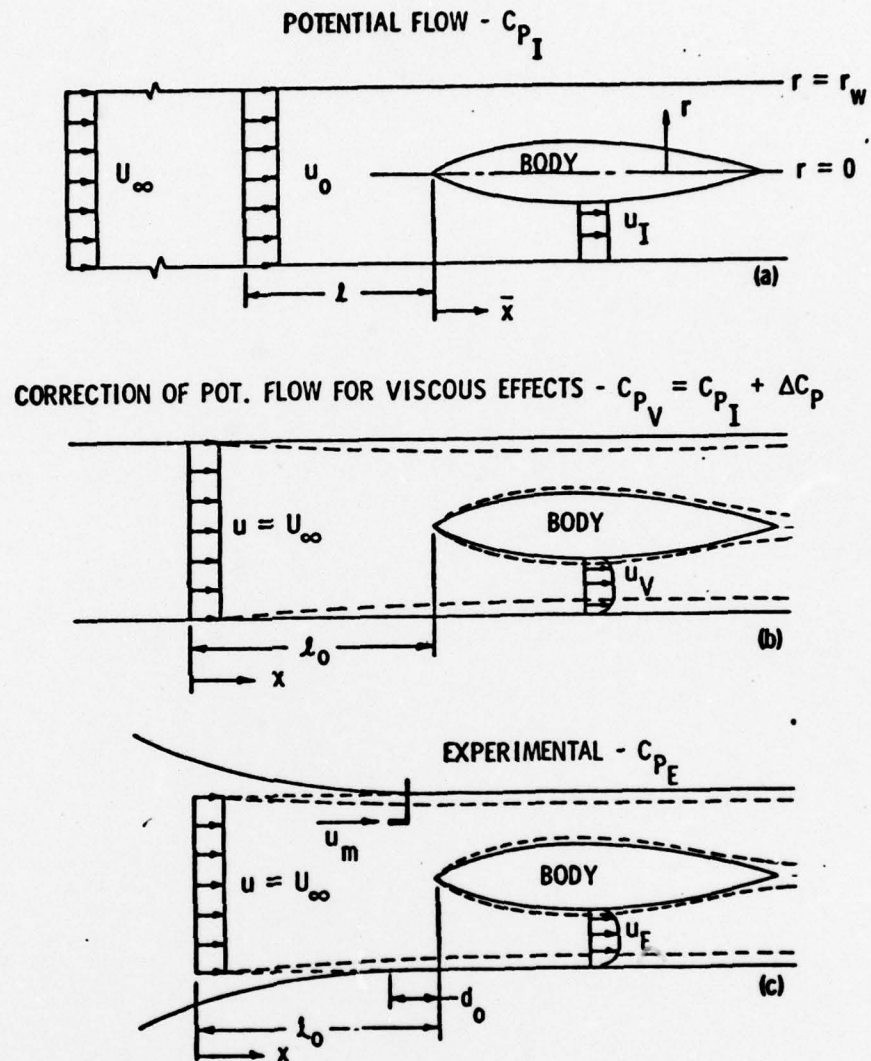


Figure 2 (a) Potential flow over a body in an infinitely long cylindrical duct, (b) a schematic description of boundary layer buildup on the body and duct wall depicting that  $u_V$  is different from  $u_I$ , and (c) a schematic description of the flow over a body in an experimental situation.

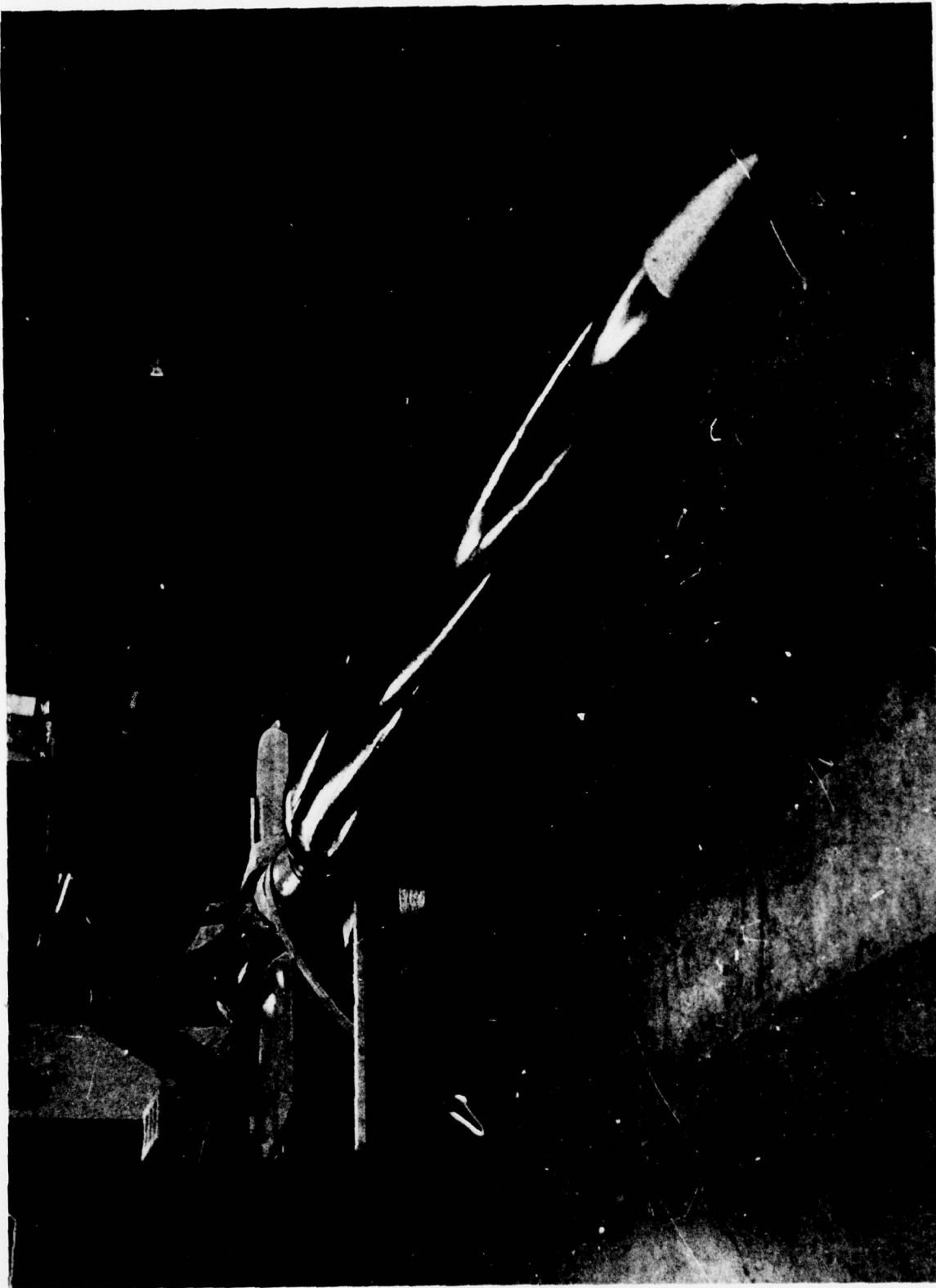


Figure 3 The body used in the experimental portion of this investigation.

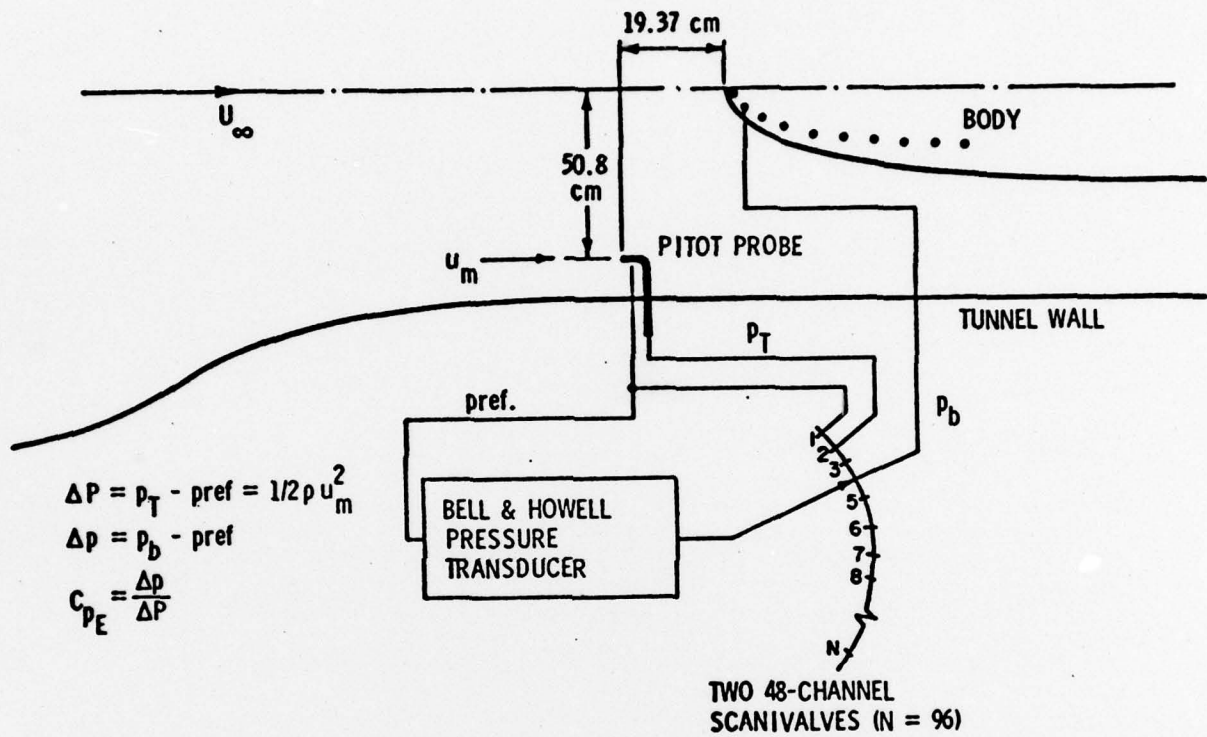


Figure 4 A schematic of the data acquisition and reduction requirements used to obtain the experimental pressure distributions.

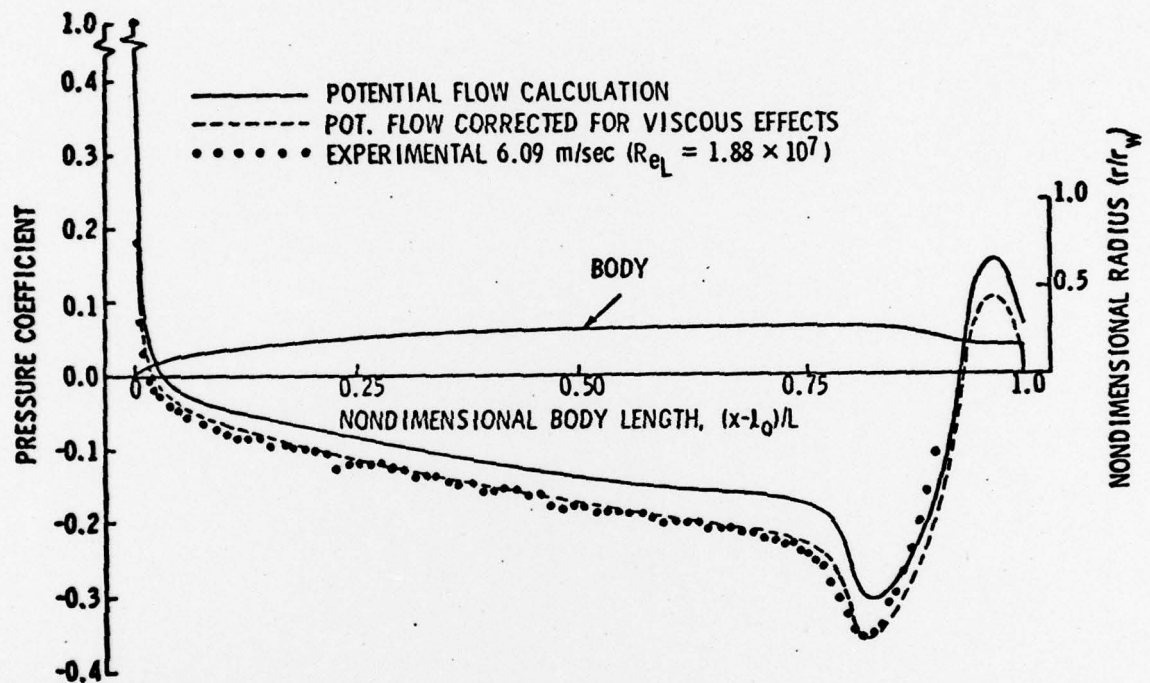


Figure 5 A comparison of the in-tunnel potential flow and corrected potential flow pressure distributions with one determined experimentally at 6.09 m./sec. in the 1.22-m. diameter water tunnel.



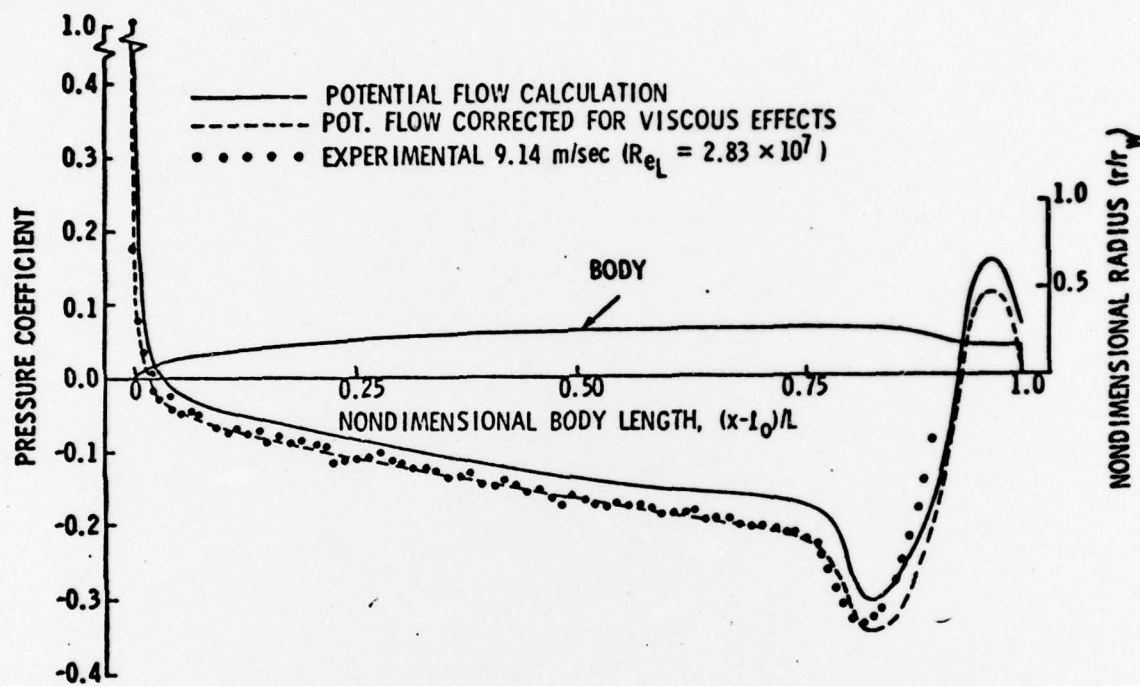


Figure 6 A comparison of the in-tunnel potential flow and corrected potential flow pressure distributions with one determined experimentally at 9.14 m./sec. in the 1.22-m. diameter water tunnel.

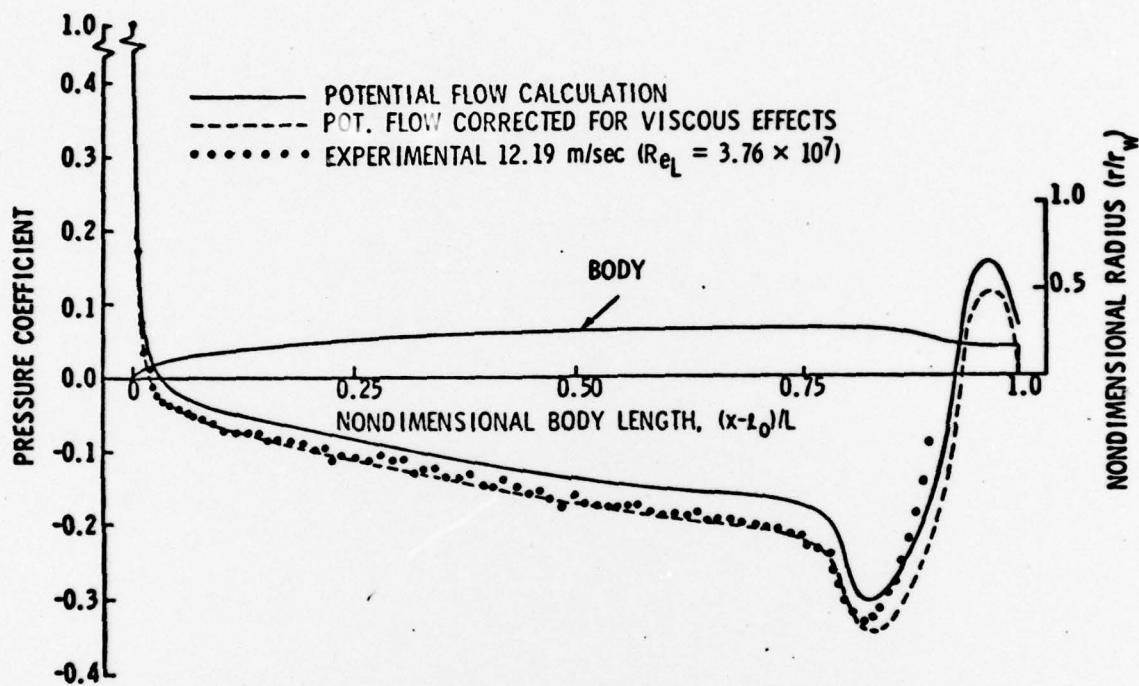


Figure 7 A comparison of the in-tunnel potential flow and corrected potential flow pressure distributions with one determined experimentally at 12.19 m./sec. in the 1.22-m. diameter water tunnel.

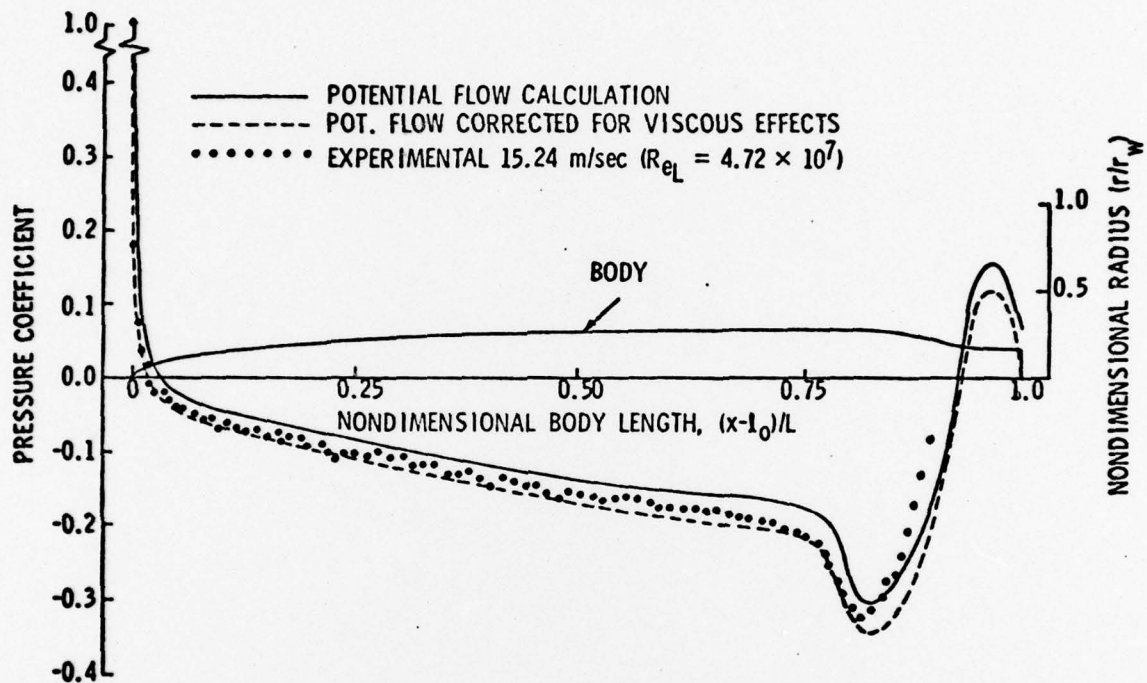


Figure 8 A comparison of the in-tunnel potential flow and corrected potential flow pressure distributions with one determined experimentally at 15.24 m./sec. in the 1.22-m. diameter water tunnel.

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